

7/4/19

Chapter - 1

Integers

Exercise 1.1

1 a. If x and y ----- y .

$$\text{Ans} = x + y = y + x$$

b. Verify ----- 44 and -36.

$$\begin{aligned}\text{Ans} = 44 - 36 &= -36 + 44 \\ 8 &= 8 \\ \text{Verified}\end{aligned}$$

2 a. Verify that $23 + (14 + 52) = (23 + 14) + 52$

$$\begin{aligned}\text{Ans} = 23 + (14 + 52) &= (23 + 14) + 52 \\ 23 + 66 &= 37 + 52 \\ 89 &= 89 \\ \text{Verified}\end{aligned}$$

b. Write the associative property of addition of integers taking a, b , and c as three integers.

$$\text{Ans} = a + (b + c) = (a + b) + c$$



3a) What is the additive identity of -6 ?

Ans: 0

b) Which integer is its own additive identity?

Ans: 0

4) Write the additive inverse of:

a) (-213)

$= +212$

b) 666

$= (-666)$

5a) Write down the integers, if any, that do not have inverse under addition.

Ans: No ^{such} integers.

b) Write down all integers that are their own inverses under addition.

Ans: 0

5 - Give a counter example to show that integers are not commutative under subtraction using:

a) 23 and -18

Ans:

$$\begin{aligned} 23 - 18 &\neq -18 - 23 \\ 23 + 18 &\neq -41 \\ 41 &\neq -41 \end{aligned}$$

b) 38 and 54

Ans:

$$\begin{aligned} 38 - 54 &\neq 54 - 38 \\ -16 &\neq 16 \end{aligned}$$

1a) Verify that: $(23 - 17) - 9 \neq 23 - (17 - 9)$

Ans:

$$\begin{aligned} (23 - 17) - 9 &\neq 23 - (17 - 9) \\ 6 - 9 &\neq 23 - 8 \\ -3 &\neq 15 \text{ Verified} \end{aligned}$$

b) Show that the associative property does not hold for integers under subtraction.

$$\begin{aligned} (15 - 17) - 6 &\neq 15 - (17 - 6) \\ -2 - 6 &\neq 15 - 9 \\ -8 &\neq 6 \end{aligned}$$

8 - Give examples of:-

a) One positive and one negative number whose sum is -18.

Ans: -19 and 1.

b) Two negative integers whose sum is



Ans: -20 and -1

c) One negative and one positive integer whose difference is -9

Ans: -1 and 18

d) Two negative numbers whose difference is 14

Ans: -1 and -15

10- The sum of two integers whose difference is 117. If one of the integers is 85, find the other.

Sum of two integers = -117
One of them = 85
Other integer = -117 - 85
= -202

11- A ----- bag

Initially, marbles in bag = 90
John took marbles = 38
Left marbles in bag = 90 - 38
= 52

Let Amit put marbles in bag = x
According to question -

$$\begin{aligned} 52 + x &= 90 + 16 \\ \Rightarrow 52 + x &= 106 \end{aligned}$$

$$\begin{aligned} \Rightarrow x &= 106 - 52 \\ \Rightarrow x &= 54 \end{aligned}$$

Amit put 54 marbles in the bag.

12-

Temperature at hill station = -4°C

Rising in temperature = 6°C

Falling in temperature = 3°C

Final temperature at hill station = (-4 + 6 - 3)°C

Ans. = -1°C

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Exercise 1.2

1 a) Give any two integers and verify the commutative property of multiplication for integers.

Ans: Let, $a = 4$ and $b = 2$

$$\Rightarrow \begin{aligned} 4 \times 2 &= 2 \times 4 \\ 8 &= 8 \end{aligned}$$

Verified

b) Give a counterexample to justify that division is not commutative for integers.

Ans: Let, $a = 4$ and $b = 2$

$$\Rightarrow \begin{aligned} 4 \div 2 &\neq 2 \div 4 \\ 2 &\neq \frac{1}{2} \end{aligned}$$

4 a) State the associative property of multiplication when for integers taking a, b, c as any three integers.

Ans: Let, $a = 4, b = 2$ and $c = 8$

$$\Rightarrow \begin{aligned} (4 \times 2) \times 8 &= 4(2 \times 8) \\ 8 \times 8 &= 4 \times 16 \\ 64 &= 64 \end{aligned}$$

b) Give a counterexample to show that division is not associative for integers.

Ans: Let, $a = 4, b = 2$ and $c = 8$

$$\Rightarrow \begin{aligned} (4 \div 2) \div 8 &\neq 4 \div (2 \div 8) \\ 2 \div 8 &\neq 4 \div \frac{1}{4} \\ \frac{1}{4} &\neq \frac{1}{4} \times \frac{1}{4} \end{aligned}$$

$$\Rightarrow \frac{1}{4} \neq \frac{1}{16}$$

5 a) Using 12, -4 and 6, prove the distributivity of subtraction.

Ans: Given addition :-

$$\Rightarrow \begin{aligned} 12 \times (-4 + 6) &= 12 \times (-4) + 12 \times 6 \\ 12 \times 2 &= -48 + 72 \\ 24 &= 24 \end{aligned}$$

Given subtraction :-

$$\Rightarrow \begin{aligned} 12 \times (-4 - 6) &\neq 12 \times (-4) - 12 \times (-6) \\ 12 \times (-10) &= -48 - 72 \\ -120 &= -120 \end{aligned}$$

b) Give a counterexample using -3 and 6 to show if division is distributive.

$$\begin{aligned} \text{Ans: } -3 \div (3 + 6) &\neq -3 \div 3 + -3 \div 6 \\ -3 \div 9 &\neq -3 + -3 \div 6 \\ -1 &\neq -3 + 1.5 \\ -1 &\neq -4.5 \end{aligned}$$

6. Evaluate:

a) $123 \times (-32)$

$= -3936$

b) $(-4) \times 39$

$= -156$

c) $(-52) \times (-9)$

$= 468$

d) 7×1

$= 7$

e) 18×0

$= 0$

f) $321 \times 1 - 61 \times 0$

$= 321 \times 1 - 0$

$\Rightarrow 321 - 0$

$\Rightarrow 321$

g) $-444 \div 27$

$= -16$

h) $576 \div (-32)$

$\Rightarrow -18$

i) $-198 \div (-17)$

$\Rightarrow 11$

j) $(-32+8) \div (-3+6)$

$\Rightarrow -24 \div (-3)$

$\Rightarrow +8$

k) $(-28+7) \times \{5-(-4)\}$

$\Rightarrow -21 \times \{5+4\}$

$\Rightarrow -21 \times 9$

$\Rightarrow -189$

l) $[-(-3) \times (7)] - [(-1) \times 2]$

$\Rightarrow [-20] - [-14]$

$\Rightarrow -21 + 14$

$\Rightarrow -7$

m) $(-15-13) \div (-12+10)$

$\Rightarrow -34 \div (-2)$

$\Rightarrow +17$

n) $(-23+8) \times [-5-(-3)]$

$\Rightarrow -25 \times (-2)$



$$0) [(-5) \times 4] - [-14 - (-6)]$$

$$\Rightarrow -20 + 18$$

$$P) (-2) \times (-2) \times (-2) \times (-2) \times (-2)$$

$$\Rightarrow +64$$

$$Q) \left(\frac{2}{3}\right) \times \left(\frac{3}{4}\right) \times \left(\frac{4}{5}\right) \times (-1) \times (-1) \times (-1) \times (-1) \times (-1) \times (-1)$$

$$\Rightarrow -1$$

8- Evaluate in a way in which the multiplication process is simplified. Also, state the properties of multiplication used in the process.

$$a) 316 \times 52$$

$$\Rightarrow 316 \times (50 + 2)$$

$$\Rightarrow 316 \times 50 + 316 \times 2$$

$$\Rightarrow 15800 + 632$$

$$\Rightarrow 16432 \text{ Distributive property is used (given addition)}$$

$$b) 76 \times 98$$

$$\Rightarrow 76 \times (100 - 2)$$

$$\Rightarrow 76 \times 100 - 76 \times 2$$

$$\Rightarrow 7600 - 152$$

$$\Rightarrow 7448$$

9- Evaluate :

$$a) (75 - 68) - [23 - (5 - 49)]$$

$$\Rightarrow 7 - [23 - 6]$$

$$\Rightarrow 7 - 17$$

$$\Rightarrow -10$$

$$b) [23 + (7 - 10)] + [(11 - 5) - (16 + 6)]$$

$$\Rightarrow [23 + -4] + [6 - 22]$$

$$\Rightarrow 19 - 16$$

$$\Rightarrow 3$$

$$c) (18 - 6) - [17 - (34 - 28) - 17]$$

$$\Rightarrow 12 - [17 - 6 - 17]$$

$$\Rightarrow 12 + 6$$

$$\Rightarrow 18$$

$$d) 44 - (34 - 40) - [(27 - 32) - 6]$$

$$\Rightarrow 44 - 6 - [-5 - 6]$$

$$\Rightarrow 50 + 11$$

$$\Rightarrow 61$$

10- A - - - - - correctly

No. of attempted Q. = 7

for no. of correct ans. = 4

No. of wrong ans. = 7 - 4

ATQ

$$d) [(-5) \times 4] - [-14 - (-6)]$$

27	-20 + 8
27	-12

p) $(-2) \times (-2) \times (-2) \times (-2) \times (-2) \times (-2)$

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q) $\begin{pmatrix} 1 \\ -1 \end{pmatrix} \times \begin{pmatrix} 1 \\ 0 \end{pmatrix} \times \begin{pmatrix} 2 \\ 1 \end{pmatrix} \times \begin{pmatrix} 1 \\ 1 \end{pmatrix} \times (-1) \times (-1) \times (-1) \times (-1) \times (-1) \times (-1) \times$

44	1
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8- Evaluate in a way in which the multiplication process is simplified. Also, state the properties of multiplication used in the process.

a) 376×52

$$\Rightarrow 376 \times (50 + 2)$$

$$\Rightarrow 376 \times 50 + 376 \times 2$$

$$\Rightarrow 18800 + 752$$

$\neq 19552$. Distribution property is used (given)

addition)

76x 98

$$\Rightarrow 76 \times (1000^2)$$

$$\Rightarrow 76 \times 100 - 76 \times 2$$

$$\begin{array}{r} 7600 - 150 \\ \hline \end{array}$$

1449

9 - Evaluando:

$$a) (75-68) - [23 - (51-45)]$$

7-123-67

主 7-17

21-7

b) $[23 + (7-1)] + [(11-5) - (16+6)]$

$$= 1 \left[\begin{smallmatrix} 23 & 4 \\ -4 & \end{smallmatrix} \right] + \left[\begin{smallmatrix} 6 & 22 \\ \end{smallmatrix} \right]$$

$$= 194.16$$

32

$$c) (13-6) - [17 - (34-28) - 17]$$

$$= 13 - [47 - 6 - 27]$$

$$= 1346$$

11	19
----	----

d) $44 - (34 - 40) - [(27 - 32) - 6]$

$$= 44 + 6 - 7 - 9 + 47 =$$

$$= 50 + 11$$

61

[illegible]

No. of attempted $Q = 7$

dot no. of selected items. = 7242

No. of wrong ans. = 7 - 1

ATC

$$\begin{aligned}
 \Rightarrow n \times 2 + (n-1) \times 1 &= 8 \\
 \Rightarrow 2n - (n-1) &= 8 \\
 \Rightarrow 2n - 1 + n &= 8 \\
 \Rightarrow 3n - 1 &= 8 \\
 \Rightarrow 3n &= 8 + 1 \\
 \Rightarrow 3n &= 9 \\
 \Rightarrow n &= \frac{9}{3} \\
 \Rightarrow n &= 3
 \end{aligned}$$

Hence, number of cement bags = 5

11- Bernam ----- cousin?

Chocolate Bernam had to deliver = 20
 she will get reward for each chocolate = ₹ 3

Esne for eating ^a chocolate = ₹ 6
 she ate chocolate = 5

Esne for eating 5 chocolate = ₹ 6 × 5 = ₹ 30

she will get reward = (20-5) × ₹ 3

$$= 15 \times ₹ 3 = ₹ 45$$

Now she will get total money = ₹ 45 + ₹ 30 = ₹ 75 Ans.

12- Shikha ----- classmates?

pencils Shikha have = 42
 she gives to each student = 5
 she gave pencils to students = 7
 the no. of pencils she gave = 7 × 5 = 35

Remaining pencils = 42 - 35 = 7 Ans.

13- Ayesha ----- treat?

Friends of Ayesha = 4
 cost of a ice cream = ₹ 12

Total cost of 4 ice creams = ₹ 12 × 4 = ₹ 48

Friends chocolate juice = 5
 cost of juice = ₹ 8

Total cost of 5 juices = ₹ 8 × 5 = ₹ 40

Total cost of all drinks = ₹ 48 + ₹ 40 = ₹ 88 Ans.

Ans 11